

Types and Patterns for Querying XML

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Language Primitives

Working on XML data requires at least two kinds of primitives:

- ② deconstruction/extraction primitives: pinpoint and capture subparts of the XML data
- ② iteration primitives: iterate over XML trees the process of extraction and transformation of data.



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Two solutions stem from *practice*:

- Path expressions
- Regular expression patterns

- 2 **iteration primitives:** iterate over XML trees the process of extraction and transformation of data.

No emerging solution: FLWR (XQuery), *select-from-where* (Cu), CQL, *select-where* (Lorel, lots-q), *filter* (XDuce), *transformers* (CDuce), in the language semantics (XSLT), ...



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Deconstructors/extractors

In running query/programming languages:

- **Paths:** "vertical" exploration of data, capture elements that may be at different depths (unary queries)
Usually XPath paths, but also the "dot" navigations (CJ, Lorel, TQL) or caterpillar expressions.
- **Regular expressions:** "horizontal" exploration of strings
Proposed by Howard Heintz for XQuery and then
generalized by CDuce/TQL, using "Caterpillar Expressions".

The two primitives are not antagonist:
they are orthogonal and complementary.



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inspired by C. Duce / CDuce (http://www.cduce.org)

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**It seems natural to integrate both of them into
a query/programming language for XML.**

Mixing horizontal and vertical selectors

Several theoretical works from *different areas* about integrating vertical and horizontal exploration:

- 1 *Unranked tree logics*: e.g. Neven&Schwentick's ETL.
- 2 *Spatial modal logics*: e.g. Cardelli&Ghelli's TQL.
- 3 *Query languages*: e.g. Papakonstantinou&Vianu's Loto-ql

But in running languages I am aware of just two examples:

• CQL (i.e. CDuce Query Language)

Paths and Regexp Patterns “coexist” but they are not integrated.



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**Opportunity of collaboration between the database
and the programming languages communities**



Outline of the talk

1 An overview of regexp types/patterns

- Patterns in functional languages
- Patterns as types with variables
- Regexp Patterns and types for XML

2 Eight reasons to consider regexp types/patterns

- Classic usages of type systems (1 2 3)
- Efficient and type precise main memory execution (4 5 6)
- Secondary memory optimization (7 8)

3 Conclusion.



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Regular expression Types and Patterns for XML



Types & patterns: the functional languages perspective

- **Types** are sets of **values**
- Values are decomposed by **patterns**
- Patterns are roughly values with **capture variables**

Instead of

```
let x = fst(e) in
let y = snd(e) in (y,x)
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with pattern one can write

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let (x,y) = e in (y,x)
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Example: tail-recursive version of length for lists:

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type List = (Any,List) | 'nil

fun length (x:(List,Int)) : Int =
  match x with
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So patterns are values with **capture variables**, **wildcards**, **constants**.

But if we:

• use for types the same constructors as for values

• use values for types and types for values

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- ① use for types the same constructors as for values
(e.g. (s,t) instead of $s \times t$)
- ② use values to denote singleton types
(e.g. `'nil` in the list type);
- ③ consider the wildcard “`_`” as synonym of `Any`



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Key idea behind regular patterns

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Patterns are types with capture variables

Define types: patterns come for free.

Which types should we start from?

Patterns are tightly connected to boolean type constructors, that is unions ($|$), intersections ($\&$) and differences (\setminus):

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To type this function we need basic types products, singletons,...

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$t ::= \text{Int} \mid v \mid (t, t) \mid t|t \mid t\&t \mid t\setminus t \mid \text{Empty} \mid \text{Any}$

but also boolean type constructors.



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Let us type the function.



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$$t = \{v \mid v \text{ value of type } t\}$$

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 (this is a type)

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(List,Int) & ('nil,Any)

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$(List,Int) \& ('nil,Any) = ('nil,Int)$

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$t = \{v \mid v \text{ value of type } t\}$ and $\{p\} = \{v \mid v \text{ matches pattern } p\}$
 (this is a type)

```
type List = (Any,List) | 'nil
```

```
fun length (x :(List,Int)) : Int =
  match x with
  | ('nil , n) -> n                               Int
  | ((_,t), n) -> length(t,n+1)
```

The first branch is executed only for values and are both in
 (List,Int) **and** in $\{('nil,n)\}$

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The second branch is executed for values that are in
 (List,Int) **not** in $\{('nil,n)\}$ **and** in $\{((_,t),n)\}$

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The second branch is executed for values that are in
 (List,Int) **not** in $\{('nil,n)\}$ **and** in $\{((_,t),n)\}$
 $((List,Int) \setminus ('nil,Any)) \& ((Any,Any), Any)$

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 $(\text{List}, \text{Int})$ **not** in $\{('nil, n)\}$ **and** in $\{((_, t), n)\}$

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The match expression has type the **union** of the possible results

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`Int | Int`

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The match expression has type the union of the possible results

`Int | Int = Int`

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```

The match expression has type the union of the possible results

$\text{Int} \mid \text{Int} = \text{Int}$

The function is well-typed

Unions, intersections, differences

- **Boolean operators are needed to type pattern matching:**

`match e with $p_1 \rightarrow e_1 \mid p_2 \rightarrow e_2$`

- To infer the type t_1 of e_1 we need $t \& \{ p_1 \}$ (where $e : t$);
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- The type of the match is $t_1 \mid t_2$.

- Boolean type constructors are useful for programming:

```
map catalogue with
  x :: (Car & (Guaranteed | (Any \ Used))) -> x
```

Select in *catalogue* all cars that if used then are guaranteed.

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match e with p1 -> e1 | p2 -> e2
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Roadmap to extend it to XML:

- 1 Define types for XML documents,
- 2 Add boolean type constructors,
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XML Types Example: A bibliography

```

type Bib = <bib>[Book*]
type Book = <book year=String>[
    Title
    (Author+ | Editor+ )
    Price?
    Publisher]
type Author = <author>[Last First]
type Editor = <editor>[Last First]
type Title = <title>[PCDATA]
type Last = <last>[PCDATA]
type First = <first>[PCDATA]
type Publisher = String
type Price = <price>[PCDATA]

```

This and: singletons, intersections, differences, Empty, and A 

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Patterns

Patterns = Types + Capture variables

TYPES

PATTERNS



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type Bib = <bib>[Book*]
```

PATTERNS



Patterns

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TYPES

```
type Bib = <bib>[Book*]
```

PATTERNS

```
<bib>[x::Book*]
```



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
```

PATTERNS

```
<bib>[x::Book*]
```

The pattern binds `x` to the *sequence* of all books in the bibliography



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
```

PATTERNS

```
match bibs with  
  <bib>[x::Book*] -> x
```



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
```

PATTERNS

```
match bibs with  
  <bib>[x::Book*] -> x
```

Returns the content of `bibs`.



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
```

PATTERNS

```
<bib>[( x::<book year="2005">_ | y::_ )]*
```



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
```

PATTERNS

```
<bib>[( x::<book year="2005">_ | y::_ )]*
```

Binds x to the sequence of all this year's books, and y to all the other books.



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
```

PATTERNS

```
match bibs with
  <bib>[( x::<book year="2005">_ | y::_ )]* -> x@y
```



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
```

PATTERNS

match bibs with

```
<bib>[( x::<book year="2005">_ | y::_ )]* -> x@y
```

Returns the concatenation (i.e., “@”) of the two captured sequences



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
type Book = <book year=String>[Title Author+ Publisher]
```

PATTERNS

```
<bib>[(x::<book year="1990">[ *_ Publisher"ACM" | _])*]
```



Patterns

Patterns = Types + Capture variables

TYPES

```
type Bib = <bib>[Book*]
type Book = <book year=String>[Title Author+ Publisher]
```

PATTERNS

```
<bib>[(x::<book year="1990">[ *_ Publisher\ "ACM" ] | _)*]
```

Binds `x` to the *sequence* of books published in 1990 from publishers others than “ACM” and discards all the others.



Patterns

Patterns = Types + Capture variables

TYPES

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type Bib = <bib>[Book*]
type Book = <book year=String>[Title Author+ Publisher]
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Returns all the captured books



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PATTERNS

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match bibs with
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```

Returns all the captured books

Exact type inference:

E.g.: if we match the pattern `[(x::Int|_)*]` against an expression of type `[Int* String Int]` the type deduced for `x` is `[Int+]`



Patterns

Patterns = Types + Capture variables

TYPES

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type Bib = <bib>[Book*]
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Returns all the captured books

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Select-from-where

Instead of just variables

```

select e from
  x1 in e1
  ⋮
  xn in en
where c

```

```

Biblio = <bib>[Book*]
Book = <book year=String>[Title (Author+|Editor+) Price?]

```



Select-from-where

Instead of just variables use patterns

```
select e from
  p1 in e1
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  pn in en
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```
Biblio = <bib>[Book*]
Book = <book year=String>[Title (Author+|Editor+) Price?]
```



Select-from-where

Instead of just variables use patterns

```
select e from
  p1 in e1
  ⋮
  pn in en
where c
```

```
<bib>[b::Book*]
<book year="1990">[ t::Title _+ <price>"69.99" ]
```

- (1) captures in `b` all the books of a bibliography
- (2) captures in `t` the title of a book if it is of 1990 and costs 69.99

```
Biblio = <bib>[Book*]
Book = <book year=String>[Title (Author+|Editor+) Price?]
```



Select-from-where

Instead of just variables use patterns

```
select e from
  p1 in e1
  ⋮
  pn in en
where c
```

```
select <book>t from
  <bib>[b::Book*] in bibs,
  <book year="1990">[ t::Title _+ <price>"69.99" ] in b
```

```
Biblio = <bib>[Book*]
```

```
Book = <book year=String>[Title (Author+|Editor+) Price?]
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Select-from-where

Instead of just variables use patterns

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select e from
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```
select <book>t from
  <bib>[b::Book*] in bibs,
  <book year="1990">[ t::Title _+ <price>"69.99" ] in b
```

Selects from **bibs** the titles of all books of 1990 and of price 69.99

```
Biblio = <bib>[Book*]
Book = <book year=String>[Title (Author+|Editor+) Price?]
```



Select-from-where

Instead of just variables use patterns

```
select e from
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where c
```

```
fun getTitles(bibs : Biblio) : [(<book>[Title])*]
  select <book>t from
    <bib>[b::Book*] in bibs,
    <book year="1990">[ t::Title _+ <price>"69.99" ] in b
```

Selects from bibs the titles of all books of 1990 and of price 69.99 and has type `Biblio -> [(<book>[Title])*]`

```
Biblio = <bib>[Book*]
Book = <book year=String>[Title (Author+|Editor+) Price?]
```



XPath encoding

For instance in CQL (...but see Xtatic for a very different encoding):

- All children of e with tag tag (e/tag)
`select x from <_ ..>[(x::(<tag ..>_)|_)]* in e`
- All attributes labelled by id ($e/@id$)
`select x from <_ id=x ..> in e`
- Notice that regexp patterns can define non-unary queries.

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Rationale

CQL, Xtatic, add syntactic sugar for XPath ...



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Rationale

CQL, Xtatic, add syntactic sugar for XPath ... **but we need more**



... it is all syntactic sugar!

Types

$$t ::= \text{Int} \mid v \mid (t, t) \mid t \vee t \mid t \wedge t \mid \neg t \mid \text{Any}$$

Patterns

$$p ::= t \mid x \mid (p, p) \mid p \vee p \mid p \wedge p$$

Example:

```
type Book = <book>[Title (Author+|Editor+) Price?]
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encoded as

$$\begin{aligned} \text{Book} &= ('book, (Title, X \vee Y)) \\ X &= (Author, X \vee (Price, 'nil) \vee 'nil) \\ Y &= (Editor, Y \vee (Price, 'nil) \vee 'nil) \end{aligned}$$


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Some reasons to consider regular expression types and patterns



Some good reasons to consider regexp patterns/types

- **Theoretical reason: very compact**
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- Classic usage
- Informative error messages
- Error mining
- Efficient execution
- Logical optimisation of pattern-based queries
- Pattern matches as building blocks for iterators
- Type/pattern-based data pruning for memory usage optimisation
- Type-based query optimisation



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- **Eight practical reasons:**
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1. Classic usages of types

Use these types as usual: static detection of errors, partial correctness, schema specification

Not much to say here, just notice that:

Singletons, unions, intersections, and differences have set-theoretic semantics on “types as set of values”: they are easy to understand.

A natural and powerful specification and constraint language:

• It is possible to specify constraints such as:

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Not very innovative but useful properties



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In case of error return a sample value in the difference of the inferred type and the expected one

List of books of a given year, stripped of the Editors and Price



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fun onlyAuthors (year:Int,books:[Book*]):[Book*] =
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type Book = <book year=String>[Title (Author+|Editor+) Price?]
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but its inferred type is:

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which is not a subtype, as shown by the sample:

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Spot subtle errors that elude current type checking technology

```
fun extract(x:[Book*]) =
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```

- Despite the type the function is well-typed:
 - The pattern is not useless, it can match authors
 - They are not regexp-patterns specific
 - Such errors are not always typical, they can be conceptual errors



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Can be formally characterised and statically detected by the types/patterns presented here and integrated in current regexp type-checkers with no overhead

4. Efficient execution

Use static type information to perform an optimal set of tests

Idea: if types tell you that something cannot happen, don't test it.

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type A = <a>[A*]  
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Computing the optimal solution requires to fully exploit intersections and differences of types

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These optimisations are orthogonal to the classical optimisations: they sum up and bring a further gain of performance

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How to define new iterators?

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Hosoya’s smart idea: Define regular expression over pattern-matches “ $p \rightarrow e$ ” (rather than over patterns).

- In-depth iterators are obtained by recursive filters
- If instead of regexp we use the core-algebra, then it is possible to define more powerful iterators.



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- In-depth iterators are obtained by recursive filters
- If instead of regexp we use the core-algebra, then it is possible to define more powerful iterators.

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Build regexp of “pattern matches” for user-defined iterators

Hosoya’s smart idea: Define regular expression over pattern-matches “ $p \rightarrow e$ ” (rather than over patterns).

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Type precision obtained by specific typing, as for patterns.

7. Type/pattern-based pruning to optimise memory usage

Use type analysis to determine which parts of an XML data need not to be loaded in main memory

Given a query q execute it on documents in which parts not necessary to evaluate q are pruned. Recently adopted in main memory XML query engines, e.g. [Marian-Jiméon], [Bressan et al.]

We can start with the notion of complement of a regular expression



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fun check(x : A|B) = match x with A -> 1 | B -> 0
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compiled as

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Data matched by wildcards “_” not in the scope of a capture variable are not necessary to the evaluation. Use boolean type constructors to determine the program data-need.

8. Type-based query optimisation

Use the precision of the type system in query optimisation

- Data description is more precise:
E.g. in IMDB there are constraints such as:
*if a show-element contains season-elements,
then its type-attribute is "TV Series".*
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- **Regex patterns start from two simple ideas:**
 - Use the same constructors for types and value
 - Define patterns as types with capture variables
- **Tightly connected with boolean combinators, make several aspects programmer-friendly:**

- **Types and values are separated**
 - and different capture variables
 - capture variables are useful for the programmer to query patterns
 - capture variables are not needed
 - Pattern and powerful type-checking language

- **Several benefits:**

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 - Concepts are easier for the programmer to understand.
 - Flexible and powerful types/queries language.
- **Several benefits:**
 - Types and patterns are easy to learn and use.
 - Types and patterns are easy to integrate with existing languages.
 - Types and patterns are easy to integrate with existing tools.



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- Regexp are good for horizontal exploration but not for vertical one. Should be integrated with path-like primitives, extended to iterators, endowed with more friendly QBE-like interfaces, ...
- I tried to give an idea about the kind of research that is pursued on XML in the programming language community but much other research goes on (security, distribution, integration in mainstream languages, streaming, ...)
- A good place to start from is PLAN-X, *ACM SIGPLAN Workshop on Programming Languages Technologies for XML*.
- To try all this install CDuce

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